## Claims

- An automated method for frequency compensated communications reception characterised in that it includes compensating for frequency offset in a received signal by adaptively forming a combination of basis functions and a training sequence that collectively approximate to a desired frequency-shifted signal to be acquired.
- A method according to Claim 1 characterised in that it includes constructing a reference signal or comparison training sequence that is an adaptively formed combination of basis functions and the training sequence.
- 3. A method according to Claim 2 for acquiring a signal with a receiver having multiple antenna elements, characterised in that the method includes constructing the reference signal by minimising a cost function constructed from an adaptively weighted combination of basis functions, a training sequence and a received signal, together with a constraint to obtain non-trivial solutions.
- 4. A method according to Claim 3 characterised in that the constraint requires non-zero signal power.
- 5. A method according to Claim 3 characterised in that the cost function is J given by:  $J = \|\mathbf{X}\mathbf{w} \mathbf{CFv}\|^2 + \lambda \left(\mathbf{w}^H \mathbf{X}^H \mathbf{X} \mathbf{w} 1\right), \text{ where } \mathbf{X} \text{ is a matrix of received signal samples, } \mathbf{w} \text{ is a vector of beamforming weights which are adaptive to minimise } J, \\ \mathbf{C} \text{ is a diagonal matrix having elements of the training sequence on its diagonal, } \mathbf{F} \\ \text{is a matrix having columns defining respective basis functions, } \mathbf{v} \text{ is a vector of weights which are adaptive to minimise } J, \text{ superscript index } H \text{ indicates a complex conjugate transpose and } \lambda \text{ is a Lagrange multiplier and the term which incorporates it is to constrain beamformer output power to be non-zero.}$
- 6. A method according to Claim 5 characterised in that it includes determining the adaptive weight vectors w and v at intervals from true estimates of a correlation matrix determined from multiple data vectors and from inverses of such estimates recursively updated to reflect successive new data vectors which are rows of the matrix X.

- 7. A method according to Claim 6 characterised in that it includes recursively updating inverse correlation matrices by:
  - forming a vector  $\mathbf{u}(n)$  having a first element  $u_1(n)$  equal to  $\sqrt{U_{1,1}(n)}$  and other elements  $u_p(n)$  (p= 2 to M) which are respective ratios  $U_{p,1}(n)/u_1(n)$ ,  $U_{p,1}(n)$  is a pth element of a first column of a matrix U(n), the matrix  $U(n) \equiv \mathbf{u}(n)\mathbf{u}^H(n) = \mathbf{x}(n)\mathbf{x}^H(n) \mathbf{x}(n-K+1)\mathbf{x}^H(n-K+1)$ ,  $\mathbf{x}(n)$  is a most recent data vector and  $\mathbf{x}(n-K+1)$  is a least recent data vector involved in updating and  $\mathbf{x}(n)\mathbf{x}^H(n)$  and  $\mathbf{x}(n-K+1)\mathbf{x}^H(n-K+1)$  are correlation matrices;
  - b) premultiplying a previous inverse correlation matrix  $\mathbf{P}(n-1)$  by vector  $\mathbf{u}^H(n)$  and postmultiplied by vector  $\mathbf{u}(n)$  to form a product and adding the product to a forget factor to form a sum;
  - c) postmultiplying the previous inverse correlation matrix P(n-1) by vector  $\mathbf{u}(n)$  and dividing by the said sum to form a quotient; and
  - d) subtracting the quotient from the previous inverse correlation matrix P(n-1) to provide a difference.
- 8. A method according to Claim 2 for acquiring a signal with a receiver having a single antenna element, characterised in that the method includes constructing the reference signal by minimising a cost function constructed from an adaptively weighted combination of basis functions, a scaled received signal and a constraint requiring non-zero signal power.
- 9. A method according to Claim 8 characterised in that the cost function is J given by:  $J = \|\mathbf{x} \mathbf{CFv}\|^2$ , where  $\mathbf{x}$  is a vector of received signal samples, and  $\mathbf{v}$ ,  $\mathbf{C}$  and  $\mathbf{F}$  are as defined earlier.
- 10. A method according to Claim 8 characterised in that the cost function is J given by:  $J = \|\alpha \mathbf{x} \mathbf{G} \mathbf{v}\|^2 + \lambda \left(\alpha^* \mathbf{x}^H \mathbf{x} \alpha 1\right), \text{ where } \alpha \text{ is a scaling factor, } \mathbf{x} \text{ is a vector of received signal samples, } \mathbf{G} \text{ is a matrix equal to } \mathbf{CF} \text{ and } \mathbf{v}, \lambda, \mathbf{C}, \mathbf{F} \text{ and } H \text{ are } \mathbf{v} = 0$

as defined earlier.

- 11. Apparatus for frequency compensated communications reception characterised in that it includes means for compensating for frequency offset in a received signal by adaptively forming a combination of basis functions and a training sequence that collectively approximate to a desired frequency-shifted signal to be acquired.
- 12. Apparatus according to Claim 11 characterised in that it includes means for constructing a reference signal or comparison training sequence that is an adaptively formed combination of basis functions and the training sequence.
- 13. Apparatus according to Claim 12 having a receiver with multiple antenna elements for acquiring the received signal, characterised in that the apparatus includes means for constructing the reference signal by minimising a cost function constructed from an adaptively weighted combination of basis functions, a training sequence and a received signal, together with a constraint to obtain non-trivial solutions.
- 14. Apparatus according to Claim 13 characterised in that the constraint requires non-zero signal power.
- 15. Apparatus according to Claim 13 characterised in that the cost function is J given by:  $J = \|\mathbf{X}\mathbf{w} \mathbf{C}\mathbf{F}\mathbf{v}\|^2 + \lambda \left(\mathbf{w}^H\mathbf{X}^H\mathbf{X}\mathbf{w} 1\right)$ , where  $\mathbf{X}$  is a matrix of received signal samples,  $\mathbf{w}$  is a vector of beamforming weights which are adaptive to minimise J,  $\mathbf{C}$  is a diagonal matrix having elements of the training sequence on its diagonal,  $\mathbf{F}$  is a matrix having columns defining respective basis functions,  $\mathbf{v}$  is a vector of weights which are adaptive to minimise J, superscript index H indicates a complex conjugate transpose and  $\lambda$  is a Lagrange multiplier and the term which incorporates it is to constrain beamformer output power to be non-zero.
- 16. Apparatus according to Claim 15 characterised in that it includes means for determining the adaptive weight vectors w and v at intervals from true estimates of a correlation matrix determined from multiple data vectors and from inverses of such estimates recursively updated to reflect successive new data vectors which are rows of the matrix X.

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- 17. Apparatus according to Claim 16 characterised in that it includes means for recursively updating inverse correlation matrices by:
  - forming a vector  $\mathbf{u}(n)$  having a first element  $\mathbf{u}_1(n)$  equal to  $\sqrt{U_{1,1}(n)}$  and other elements  $\mathbf{u}_p(n)$  (p= 2 to M) which are respective ratios  $U_{p,1}(n)/\mathbf{u}_1(n)$ ,  $U_{p,1}(n)$  is a pth element of a first column of a matrix  $\mathbf{U}(n)$ , the matrix  $\mathbf{U}(n) \equiv \mathbf{u}(n)\mathbf{u}^H(n) = \mathbf{x}(n)\mathbf{x}^H(n) \mathbf{x}(n-K+1)\mathbf{x}^H(n-K+1)$ ,  $\mathbf{x}(n)$  is a most recent data vector and  $\mathbf{x}(n-K+1)$  is a least recent data vector involved in updating and  $\mathbf{x}(n)\mathbf{x}^H(n)$  and  $\mathbf{x}(n-K+1)\mathbf{x}^H(n-K+1)$  are correlation matrices;
  - b) premultiplying a previous inverse correlation matrix  $\mathbf{P}(n-1)$  by vector  $\mathbf{u}^H(n)$  and postmultiplied by vector  $\mathbf{u}(n)$  to form a product and adding the product to a forget factor to form a sum;
  - c) postmultiplying the previous inverse correlation matrix P(n-1) by vector  $\mathbf{u}(n)$  and dividing by the said sum to form a quotient; and
  - d) subtracting the quotient from the previous inverse correlation matrix P(n-1) to provide a difference.
- 18. Apparatus according to Claim 12 having a receiver with a single antenna element for acquiring the received signal, characterised in that the apparatus includes means for constructing the reference signal by minimising a cost function constructed from an adaptively weighted combination of basis functions, a scaled received signal and a constraint requiring non-zero signal power.
- Apparatus according to Claim 18 characterised in that the cost function is J given by:  $J = \|\mathbf{x} \mathbf{CFv}\|^2$ , where  $\mathbf{x}$  is a vector of received signal samples, and  $\mathbf{v}$ ,  $\mathbf{C}$  and  $\mathbf{F}$  are as defined earlier.
- 20. Apparatus according to Claim 18 characterised in that the cost function is J given by:  $J = \|\alpha \mathbf{x} \mathbf{G} \mathbf{v}\|^2 + \lambda \left(\alpha^* \mathbf{x}^H \mathbf{x} \alpha 1\right)$ , where  $\alpha$  is a scaling factor,  $\mathbf{x}$  is a vector of received signal samples,  $\mathbf{G}$  is a matrix equal to  $\mathbf{CF}$  and  $\mathbf{v}$ ,  $\lambda$ ,  $\mathbf{C}$ ,  $\mathbf{F}$  and H are

as defined earlier.

- 21. Computer software for controlling a computer processor and for use in frequency compensated communications reception characterised in that it includes program code instructions for compensating for frequency offset in a received signal by adaptively forming a combination of basis functions and a training sequence that collectively approximate to a desired frequency-shifted signal to be acquired.
- 22. Computer software according to Claim 21 characterised in that it includes program code instructions for constructing a reference signal or comparison training sequence that is an adaptively formed combination of basis functions and the training sequence.
- 23. Computer software according to Claim 22 for use in processing received signals acquired by a receiver with multiple antenna elements, characterised in that the computer software includes program code instructions for constructing the reference signal by minimising a cost function constructed from an adaptively weighted combination of basis functions, a training sequence and a received signal, together with a constraint to obtain non-trivial solutions.
- 24. Computer software according to Claim 23 characterised in that the constraint requires non-zero signal power.
- Computer software according to Claim 23 characterised in that the cost function is J given by:  $J = \|\mathbf{X}\mathbf{w} \mathbf{CF}\mathbf{v}\|^2 + \lambda \left(\mathbf{w}^H\mathbf{X}^H\mathbf{X}\mathbf{w} 1\right)$ , where  $\mathbf{X}$  is a matrix of received signal samples,  $\mathbf{w}$  is a vector of beamforming weights which are adaptive to minimise J,  $\mathbf{C}$  is a diagonal matrix having elements of the training sequence on its diagonal,  $\mathbf{F}$  is a matrix having columns defining respective basis functions,  $\mathbf{v}$  is a vector of weights which are adaptive to minimise J, superscript index H indicates a complex conjugate transpose and  $\lambda$  is a Lagrange multiplier and the term which incorporates it is to constrain beamformer output power to be non-zero.
- 26. Computer software according to Claim 25 characterised in that it includes program code instructions for determining the adaptive weight vectors w and v at intervals from true estimates of a correlation matrix determined from multiple data vectors

and from inverses of such estimates recursively updated to reflect successive new data vectors which are rows of the matrix  $\mathbf{X}$ .

- 27. Computer software according to Claim 26 characterised in that it includes program code instructions for recursively updating inverse correlation matrices by:
  - forming a vector  $\mathbf{u}(n)$  having a first element  $\mathbf{u}_1(n)$  equal to  $\sqrt{U_{1,1}(n)}$  and other elements  $\mathbf{u}_p(n)$  (p= 2 to M) which are respective ratios  $\mathbf{U}_{p,1}(n)/\mathbf{u}_1(n)$ ,  $\mathbf{U}_{p,1}(n)$  is a pth element of a first column of a matrix  $\mathbf{U}(n)$ , the matrix  $\mathbf{U}(n) \equiv \mathbf{u}(n)\mathbf{u}^H(n) = \mathbf{x}(n)\mathbf{x}^H(n) \mathbf{x}(n-K+1)\mathbf{x}^H(n-K+1)$ ,  $\mathbf{x}(n)$  is a most recent data vector and  $\mathbf{x}(n-K+1)$  is a least recent data vector involved in updating and  $\mathbf{x}(n)\mathbf{x}^H(n)$  and  $\mathbf{x}(n-K+1)\mathbf{x}^H(n-K+1)$  are correlation matrices;
  - b) premultiplying a previous inverse correlation matrix  $\mathbf{P}(n-1)$  by vector  $\mathbf{u}^H(n)$  and postmultiplied by vector  $\mathbf{u}(n)$  to form a product and adding the product to a forget factor to form a sum;
  - c) postmultiplying the previous inverse correlation matrix P(n-1) by vector  $\mathbf{u}(n)$  and dividing by the said sum to form a quotient; and
  - d) subtracting the quotient from the previous inverse correlation matrix  $\mathbf{P}(n-1)$  to provide a difference.
- 28. Computer software according to Claim 22 for use in processing received signals acquired by a receiver with a single antenna element, characterised in that the computer software includes program code instructions for constructing the reference signal by minimising a cost function constructed from an adaptively weighted combination of basis functions, a scaled received signal and a constraint requiring non-zero signal power.
- Computer software according to Claim 28 characterised in that the cost function is J given by:  $J = \|\mathbf{x} \mathbf{CFv}\|^2$ , where  $\mathbf{x}$  is a vector of received signal samples, and  $\mathbf{v}$ ,  $\mathbf{C}$  and  $\mathbf{F}$  are as defined earlier.

30. Computer software according to Claim 28 characterised in that the cost function is J given by:  $J = \|\alpha \mathbf{x} - \mathbf{G} \mathbf{v}\|^2 + \lambda \left(\alpha^* \mathbf{x}^H \mathbf{x} \alpha - 1\right)$ , where  $\alpha$  is a scaling factor,  $\mathbf{x}$  is a vector of received signal samples,  $\mathbf{G}$  is a matrix equal to  $\mathbf{CF}$  and  $\mathbf{v}$ ,  $\lambda$ ,  $\mathbf{C}$ ,  $\mathbf{F}$  and H are as defined earlier.